

$$c^2 = a^2 + b^2 - 2ab \cos C$$

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Horizontally: $T_{1x} = T_{2x}$

$$T_1 \cos \alpha = T_2 \cos \beta$$

Vertically: $T_{1y} + T_{2y} = F_g$

$$T_1 \sin \alpha + T_2 \sin \beta = F_g$$

Conservation of Momentum in 2D

- Recall that momentum was conserved in 1D (neglecting friction).
- Recall: $\vec{p} = m\vec{v}$

Law of Conservation of Momentum

$$\vec{p}_A + \vec{p}_B = \vec{p}'_A + \vec{p}'_B$$

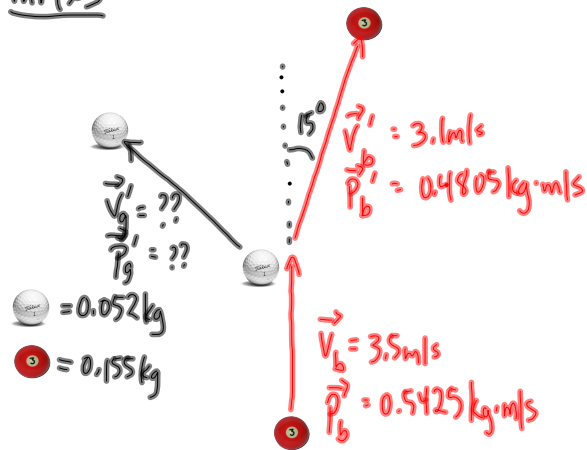
total momentum = total momentum
before after

$$\vec{p}_{\text{total}} = \vec{p}'_{\text{total}}$$

$$p_{x\text{total}} = p'_{x\text{total}}$$

$$p_{y\text{total}} = p'_{y\text{total}}$$

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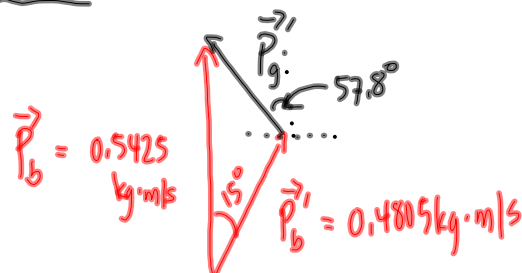
According to the Law of Conservation of Momentum:

$$\vec{P}_{total} = \vec{P}'_{total}$$

$$\vec{P}_b + \vec{P}_g = \vec{P}'_b + \vec{P}'_g$$

$$\vec{P}_b = \vec{P}'_b + \vec{P}'_g$$

OPTION A - Draw a Vector Addition Diagram



$$c^2 = a^2 + b^2 - 2ab \cos C$$

$$c^2 = (0.4805)^2 + (0.5425)^2 - 2(0.4805)(0.5425) \cos 15^\circ$$

$$c = 0.147 \text{ kg}\cdot\text{m/s}$$

$$\frac{a}{\sin A} = \frac{b}{\sin B}$$

$$\vec{P}'_g = 0.147 \text{ kg}\cdot\text{m/s} \left[57.8^\circ \text{ ccw from original dir of bill. ball} \right]$$

$$\frac{0.147}{\sin 15^\circ} = \frac{0.4805}{\sin \beta}$$

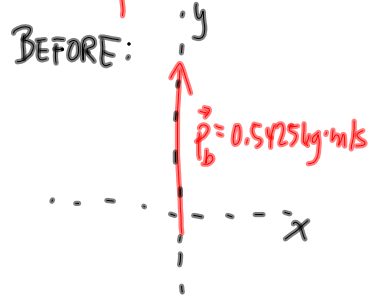
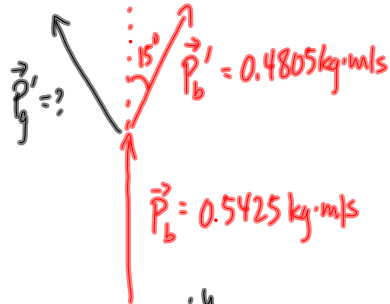
$$\vec{V}'_g = \frac{0.147 \text{ kg}\cdot\text{m/s}}{0.052 \text{ kg}} \left[57.8^\circ \dots \right]$$

$$\sin \beta = \frac{0.4805 \sin 15^\circ}{0.147}$$

$$\beta = 57.8^\circ$$

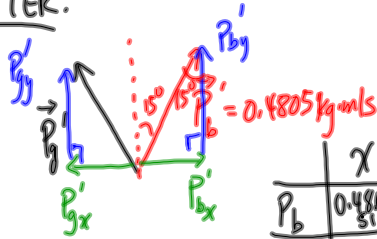
$$\vec{V}_g = 2.8 \text{ m/s} \left[58^\circ \dots \right]$$

OPTION B - use components (x-y chart BEFORE + AFTER)



	x	y
P_b	0	0.5425
P_g	0	0
P_{total}	0	0.5425

AFTER:



	x	y
P_b	$0.4805 \sin 15^\circ$	$0.4805 \cos 15^\circ$
P_g	x	y
P_{total}	0	0.5425

x-components:

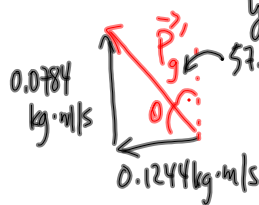
$$0.4805 \sin 15^\circ + x = 0$$

$$x = -0.1244 \text{ kg}\cdot\text{m/s}$$

y-components:

$$0.4805 \cos 15^\circ + y = 0.5425$$

$$y = 0.0784 \text{ kg}\cdot\text{m/s}$$



$$P_g' = 0.147 \text{ kg}\cdot\text{m/s}$$

$$\tan \theta = \frac{0.0784}{0.1244}$$

$$\theta = 32.2^\circ$$

Same answer as before.

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